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Examining the relationships between phenotypic plasticity and local	2
environments with genomic structural equation models	3
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Abstract

Environmental association analyses (EAA) seek to identify genetic variants associated with local	21
adaptation by regressing local environmental conditions at collection sites on genome-wide	22
polymorphisms. The rationale is that environmental conditions impose selective pressure on trait(s), and	23
these traits are regulated in part by variation at a genomic level. Here, we present an alternative	24
multivariate genomic approach that can be utilized when both phenotypic and environmental data are	25
available for the population. This framework utilizes Bayesian networks (BN) to elucidate	26
interdependancies between local environmental conditions and empirical phenotypes, and jointly	27
estimates the direct and indirect genetic covariances between empirical phenotypes and environmental	28
conditions using a mixed-effects structural equation model (SEM). Direct genomic covariance between	29
empirical phenotypes and environmental conditions may provide insight into whether QTL that affect	30
adaptation to an environmental gradient also affects the observed phenotype. To demonstrate the utility	31
of this approach, we leveraged two existing datasets consisting of 55 climate variables for $1,130$	32
Arabidopsis accessions and empirical phenotypes for fitness and phenology collected on 515 accessions in	33
two common garden locations in Europe. BN showed that plasticity for fitness and phenology was highly	34
dependant on local environmental conditions. Moreover, genomic SEM revealed relatively high positive	35
genomic correlation between plasticity in fitness and environmental variables that describe the	36
favorability of the local environment for plant growth, indicating the presence of common QTL or	37
independent QTL that are tightly linked. We believe the frameworks presented in this manuscript can	38
provide new insights into the genetic basis of local adaptation.	39

Introduction

Identifying traits that confer adaptation to a given environment and elucidating the genetic determinants 41 driving variation for these traits is an important goal for physiologists, evolutionary biologists, and 42 quantitative geneticists. In many cases, particularly those working with agronomic species, these studies 43 involve large-scale phenotypic evaluations in multiple environments, which are later integrated with genomic data using quantitative genetic frameworks. However, when the population is composed of individuals sampled across an environmental gradient, information regarding local environmental conditions at collection sites can be leveraged together with genomic data to identify genetic variants 47 associated with variation for a given environmental factor (Fournier-Level et al., 2011; Blanquart et al., 48 2013; Yoder et al., 2014; Tiffin and Ross-Ibarra, 2014; Hoban et al., 2016). In recent years, a number of 49 studies have employed similar approaches, termed environmental association analysis (EAA), to study 50 the genetic basis of local adaptation (Fournier-Level et al., 2011; Yoder et al., 2014; Lasky et al., 2015). 51

EAA seeks to identify genomic variants that are associated with variation in environmental 52 conditions at collection sites (Jones et al., 2013; Dell'Acqua et al., 2014; Yoder et al., 2014; Lasky et al., 53 2015; Anderson et al., 2016). The rationale for these approaches is that local environmental conditions impose selective pressure on some trait(s), and these traits are regulated in part by variation at a 55 genomic level. Since adaptive traits should be correlated with local environmental conditions, regression 56 of environmental variables on genome-wide single nucleotide polymorphisms (SNPs) may vield markers 57 that are associated with environmental variables and, by proxy, adaptive traits. Several studies have leveraged these, and similar approaches, to elucidate the genetic basis of local adaptation (Fournier-Level 59 et al., 2011; Yoder et al., 2014; Lasky et al., 2015). The only requirements for EAA is genomic data for a 60 georeferenced population and environmental variables recorded at, or close to, collection sites. 61 Downstream analyses or independent studies are performed to determine if these variants have an effect 62 on the phenotype, or whether they can be used to predict phenotypic variation. For instance, Yoder et al. 63 (2014) utilized a population of 202 wild *Medicago truncatula* accessions to identify genomic associations 64 with annual mean temperature, precipitation in the wettest month, and isothermality. They showed that 65 accessions with a greater number of alleles associated with high precipitation in the wettest month also 66 exhibited higher growth rate in a wet controlled environment. Similarly, Lasky et al. (2015) first 67 identified environment-genotype associations in a panel of Sorghum landraces, and used these 68 associations to predict agronomic characteristics in environments with contrasting moisture or edaphic 69 conditions. Thus, these studies provide evidence that EAA can recover genetic determinate that are 70 associated with environmental adaptation, and may influence phenotypic variation for adaptive or 71 agronomically relevant traits. 72

However, when both phenotypic and environmental data are available for the population, alternative 73 multivariate approaches can be utilized to jointly estimate genomic parameters and elucidate the genetic 74

interrelationships between local environmental conditions and observable phenotypes. With these 75 approaches we can address whether there is a dependancy between the empirical phenotype and the local environmental condition, effectively addressing the question "Is local adaptation to an environmental 77 variable dependant on this trait?" and "What genes have an impact on both local adaptation and the 78 empirical phenotype?" Structural equation models (SEM) are powerful frameworks that can be used to 79 model the interdependancies between multiple variables (Wright, 1921; Haavelmo, 1943). When 80 integrated into a quantitative genetics framework, these approaches allow quantitative genetic loci (QTL) 81 or total genomic values to be decomposed into direct and indirect effects based on a predefined graphical 82 model that describes directed relationships between variables (Gianola and Sorensen, 2004; Valente et al., 83 2013). SEM can be viewed as an extension of a conventional multi-trait (MT) quantitative genetic 84 framework (Valente et al., 2013). Whereas with MT approaches, covariances among observable 85 phenotypes are estimated and used to describe the symmetric linear relationships between variables, SEM extends the multivariate framework to allow recursive (effects from one phenotype affects the 87 outcome of another) and simultaneous (reciprocal) structures among its variables by utilizing phenotypes 88 as predictors for other phenotypes (Goldberger, 1972; Bielby and Hauser, 1977). 89

In quantitative genetics, SEM has been largely applied to topics in animal breeding and genetics. For 90 instance in one of the first applications of SEM in quantitative genetics in the context of a linear mixed model, de los Campos et al. (2006b) used SEM to elucidate the interrelationship between milk yield and 92 mastitis (inflammation of the udder quantified using somatic cell scores) in dairy cattle. The authors 93 showed that models where milk yield was dependent on mastitis were better supported by the data. 94 indicating that disease was the primary driver of reduced milk production rather than the converse. 95 Since this work, quantitative genetic SEM frameworks have been used to elucidate the genetic interdependencies among meat quality traits, calving traits, fertility metrics, as well as milk yield and 97 mastitis in other species or breeds (de los Campos et al., 2006a,b; Varona et al., 2007; Wu et al., 2007; 98 König et al., 2008; Heringstad et al., 2009; de Maturana et al., 2009, 2010; Jamrozik et al., 2010; qq Peñagaricano et al., 2015a,b). More recently, the SEM quantitative genetic frameworks have been 100 extended to perform genome-wide associations in chicken and rice (Momen et al., 2018, 2019). Given 101 that many EAA studies assume a causal relationship between an unobserved phenotype and the local 102 environment, SEM provides a framework where in these relationships can be explicitly encoded in the 103 model – when empirical phenotypes are available for the same population. Moreover, these frameworks 104 provide a means to examine the covariance in genetic effects that act directly on the empirical phenotype 105 and the environmental variable (Valente et al., 2013). 106

Direct applications of quantitative genetic SEM frameworks to EAA is not trivial. For one, SEM 107 requires a putative causal networks that describes the dependancies among and between environmental 108 variables and empirical phenotypes (Gianola and Sorensen, 2004). In most cases, these networks are not 109

only unknown, but learning the structure may even be an objective of the study itself. Secondly, the 110 environmental data often consist of dozens or hundreds of variables that are highly correlated 111 (Ferrero-Serrano and Assmann, 2019; Lasky et al., 2015). Thus, prior to applying SEM to EAA we must 112 reduce the dimensionality of the environmental data and determine an appropriate network structure. 113 One popular approach for dimensional reduction is factor analysis (FA) (de Los Campos and Gianola, 114 2007). The underlying rationale for FA is that relationships among variables are due to some underlying 115 unobserved process. The goal of FA is to define a reduced set of unobserved, latent variables that 116 maximize the correlation among groups of related observed variables. In quantitative genetics, FA is 117 routinely applied to multi-environmental trials and high-dimensional multi-trait applications (Kelly 118 et al., 2007; Meyer, 2009; de Los Campos and Gianola, 2007; Runcie and Mukherjee, 2013; Yu et al., 119 2019). Thus, when applied to high dimensional environmental data, FA may yield a reduced set of 120 underlying variables that capture major patterns of local environments. When the underlying causal 121 structure is unknown, Bayesian network (BN) approaches can be utilized to elucidate the probabilistic 122 dependencies among variables (Scutari, 2009; Scutari and Denis, 2014). These dependencies are 123 expressed using a directed acyclic graph where each variable is depicted as a node and directed edges 124 join dependant nodes. Although BN approaches learn dependencies from the data itself, these 125 approaches can yield insightful information regarding the causal relationships among variables. Such 126 approaches have been leveraged to understand the genetic interdependencies among complex traits and 127 have been utilized to elucidate potential causal structures that can be used in SEM quantitative genetic 128 frameworks (Valente et al., 2013; Yu et al., 2019; Momen et al., 2018, 2019). Thus, both FA and BN can 129 be leveraged to reduce the dimensionality of local environmental variables and elucidate the relations 130 between traits or latent factors. 131

The objective of this study is to demonstrate the utility of SEM quantitative genetic frameworks for 132 studying the genetic interrelationships between local environmental conditions and empirical phenotypes 133 associated with fitness and phenology. To this end, we utilized two publicly available data sets that 134 describe environmental variables at collection sites for 1,130 diverse Arabidopis thaliana accessions, and 135 empirical phenotypes in two precipitation regimes at two common garden locations in Europe 136 (Ferrero-Serrano and Assmann, 2019; Exposito-Alonso et al., 2019). Several studies have shown that 137 adaptation is polygenic (Pritchard and Di Rienzo, 2010; Pritchard et al., 2010; Flood and Hancock, 138 2017). With this in mind, we sought to forego single marker inferences and instead predict total genomic 139 values for each individual, which are the cumulative additive genetic value for a given phenotypic 140 variable. We seek to decompose total genetic effects for these variables into direct and indirect effects, 141 effectively allowing us to address the following questions: "Are genetic effects for empirical phenotypes 142 dependant on the genetic drivers for adaptation to local environmental conditions (and vice versa)?" and 143 "How much of the total genomic value for an empirical phenotype is due to genetic effects from upstream 144

phenotypic variables?".

Materials and Methods

Environmental variables

This study utilized a publicly available data set of local environmental conditions for 1,130 Arabidopsis ¹⁴⁸ accessions. The original data, compiled by Ferrero-Serrano and Assmann (2019), consisted of 205 ¹⁴⁹ environmental variables for 829 unique collection sites. Categorical variables were removed from the data ¹⁵⁰ set, as well as variables that had missing values in $\geq 20\%$ of the accessions. After this filtering, 139 ¹⁵¹ climate variables remained. Prior to FA, we removed variables that showed high collinearity, as variables ¹⁵² with very high correlation can interfere with factor analysis. In total, these quality control steps provided ¹⁵³ data for 55 environmental variables for 1,130 accessions. ¹⁵⁴

Empirical Phenotypes

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Since the objective of the study was to examine the genomic interrelationships between local climate 156 conditions and phenotypic plasticity in contrasting environments, we sought a data set that provided 157 phenotypes recorded in the same germplasm in contrasting and ecologically-relevant conditions. To this 158 end, we used data from a recent study by Exposito-Alonso et al. (2019) in which 515 of the 1,130 159 accessions were phenotyped for fitness, germination time and flowering time in two locations within the 160 natural range of Arabidopsis thaliana and two simulated precipitation regimes. The experimental design 161 and collection of phenotypic data is explained in great detail by Exposito-Alonso et al. (2019). Briefly, 162 the 515 accessions were grown in open-ended rain-out shelters in Tuebingen, Germany and Madrid, 163 Spain. The open-ended design allows for the temperature and humidity conditions within the structure 164 to be similar to the natural environment. Within each location the plants were grown in a split-plot 165 design. Two simulated precipitation regimes, which were designed to mimic natural rainfall at Tuebingen 166 and Madrid, were randomly assigned to each subplot. The interquartile range for soil water content 167 (SWC) in the low-precipitation treatment was 11.38-22.51% with a median of 16.1% in Madrid and 168 10.76-20.09% with a median of 14.7% in Tuebingen. The interquartile range for the high precipitation 169 regime was 20.73-29.02% with a median of 24.6% in Madrid, and 22.62-33.00% with a median of 27.8%170 in Tuebingen. Median midday photosynthetically active radiation (PAR) values inside the shelters were 171 $45.7 \text{ mol}\cdot\text{m}^{-2}\cdot\text{day}^{-1}$ in Madrid and $30.9 \text{ mol}\cdot\text{m}^{-2}\cdot\text{day}^{-1}$ in Tuebingen. Temperatures outside the 172 structures ranged from 5.34-12.39°C with a median of 8.5°C in Madrid and 2.44-9.54°C with a median of 173 5.6° C in Tuebingen. These ranges are very consistent with temperatures recorded in the structures 174 (Exposito-Alonso et al., 2019). 175

We estimated the macroenvironmental sensitivity for each accession and each empirical phenotype that was recorded by Exposito-Alonso et al. (2019) using the Finlay-Wilkinson (FW) approach (Finlay and Wilkinson, 1963). FW essentially expresses the plasticity of an accession grown across multiple

environments as a function of the overall population performance in each environment. The FW model is given by

$$y_{ij} = \mu + g_i + E_j + h_i E_j + e_{ij}$$

where y_{ij} is the phenotype for accession *i* in environment *j*, μ is the overall mean, g_i is the main accession effect, E_j is the main environment effect, h_i is the slope for accession *i* on the overall environment means, and e_{ij} is the residual for accession *i* in environment *j*. Here, y_{ij} are best linear unbiased estimates for the accession effect in each environment from a model that accounts for systematic experimental effects (Exposito-Alonso et al., 2019). The FW model was fit using the FW package in R (Lian, 2014). The slope from this model was used as a metric for phenotypic plasticity in all downstream analysis.

Genotyping data

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Imputed SNP markers were obtained for all 1,135 accessions from 1001genomes 183 (https://1001genomes.org/data/GMI-MPI/releases/v3.1/SNP_matrix_imputed_hdf5/) (Weigel 184 and Mott, 2009; Alonso-Blanco et al., 2016). We extracted marker information for the 1,130 accessions 185 with climate data, and removed SNPs with low minor allele frequencies (MAF < 0.05). Moreover, SNPs 186 in high linkage disequilibrium (LD) (r > 0.85) were removed using the PLINK indep function with a 50 187 SNP window, a step size of 5 SNPs, and a variance inflation factor (VIF) of 3.6. The VIF is computed as 188 $\frac{1}{1-r^2}$. Thus, a VIF of 3.6 corresponds to a $r \approx 0.85$. After these filtering steps, 426,567 SNPs remained. 189

Factor analysis of environmental variables

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To reduce the dimensionality of the 55 environmental variables, and define a reduced subset that ¹⁹¹ captures potential undefined/unobserved variables that give rise to the original covariance, we utilized a ¹⁹² combination of FA techniques, specifically exploratory and confirmatory factor analysis (EFA and CFA, ¹⁹³ respectively). Factor analysis seeks to identify a smaller set of latent variables that capture the ¹⁹⁴ underlying interrelationships between the original, manifest variables. The relationships between latent ¹⁹⁵ and manifest variables is given by ¹⁹⁶

$$\mathbf{Y} = \mathbf{\Gamma}\mathbf{F} + \mathbf{s} \tag{1}$$

where **Y** is an $t \times n$ matrix of phenotypes with n = 515 indicating the number of accessions and t = 55indicating the number of traits; **F** is an $l \times n$ matrix of factor scores that describe the values for each latent factor (l) for each accession; **Γ** is an $t \times l$ matrix that shows how each trait (t) loads onto each latent factor; and **s** is a $t \times n$ matrix that represents the specific effects for each trait and accession. Thus, FA expresses a set of manifest variables as a function of common, latent factors.

While both EFA and CFA are based on a similar framework, EFA allows manifest variables to load 202 onto multiple latent factors and CFA does not. Thus, EFA is most often used to determine the 203 appropriate number of latent factors and examine how manifest variables load on to them, and CFA is 204 used to test hypothesis regarding the relationships between manifest and latent factors and to estimate 205 factor loading scores. We determined the appropriate number of factors using parallel analysis. Parallel 206 analysis is a simulation-based method that was originally proposed by Horn (1965) to determine the 207 optimal number of latent factors. Briefly, parallel analysis randomly simulates data sets with similar 208 properties to the observed data and uses these data to extract eigenvalues. Scree plots are used to plot 209 and compare eigenvalues from the simulated data and eigenvalues from the observed data. The optimal 210 number of factors is determined as the maximum number of factors that have observed eigenvalues that 211 are larger than eigenvalues from simulated data. Parallel analysis was performed using the fa.parallel 212 function in the psych package R (Revelle, 2018). We used the minimum residual method with 1,000 213 iterations. Once the optimal number of factors was determined (11 latent factors), EFA was performed 214 using the factor analysis function, fa(), with varimax rotation and the minimum residual method with 215 1,000 iterations. 216

CFA was used to estimate factor scores for each accession and latent environmental variable. Since ²¹⁷ CFA only allows manifest variables to load onto a single latent variable, we used EFA results to determine ²¹⁸ which latent factor had the largest absolute loading for each manifest variable. Although EFA identified ²¹⁹ 11 latent factors, one latent factor was omitted from CFA because all manifest variables that loaded onto ²²⁰ this latent factor had higher loadings for other latent factors. CFA was fit using the **sem** package in R ²²¹ according to the loadings provided in Figure 1 (Fox et al., 2017). Factor scores were computed with the ²²² 'regression' method using the **fscores**() function in the **sem** package (Fox et al., 2017). ²²³

Structure learning using Bayesian network

We next sought to elucidate the genomic interrelationships between plasticity and latent factor scores from CFA for local environmental conditions following an approach described by Yu et al. (2019). To this end, we first predicted genomic values for each accession and trait using a Bayesian multi-trait model (MTM). The MTM is given by

$$Y = Xb + Zu + e$$

where \mathbf{Y} is an $n \times t'$ matrix of phenotypes composed of factor scores for latent environmental factors and plasticity for empirical phenotypes (t' = 13), where n = 515 is the number of individuals and t' is the number of phenotypes (ten latent local environmental variables and three empirical phenotypes, t' = 13); \mathbf{X} and \mathbf{Z} are incidence matrices that relate phenotypes to vectors of systematic effects (**b**) and additive genetic effects **u**, respectively; and **e** is the error term. Moreover, we assume $\mathbf{u} \sim N(0, \boldsymbol{\Sigma}_{\mathbf{u}} \otimes \mathbf{G})$ and $\mathbf{e} \sim N(0, \boldsymbol{\Sigma}_{\mathbf{e}} \otimes \mathbf{I}_{n \times n})$, where **G** is a genomic relationship matrix constructed following VanRaden (2008), 230

 Σ_{u} is a $t' \times t'$ covariance matrix for additive genetic effects. The MTM was fit using the MTM package in R with 10,000 Markov chain Monte-carlo (MCMC) samples of which the first 2,000 are discarded and every fifth sample was retained (de los Campos and Grüneberg, 2016).

Bayesian network (BN) learning approaches assume that the samples are independent. However, 234 when predicting additive genomic values using MTM, dependencies are between breeding values for 235 accessions are introduced from **G**. Therefore prior to BN learning, we followed an approach described by 236 Töpner et al. (2017) to remove dependencies. Briefly, G was decomposed into Cholesky factors by 237 $\mathbf{G} = \mathbf{L}\mathbf{L}'$, where \mathbf{L} is a lower triangle matrix with dimensions $n \times n$. We define a $nt' \times nt'$ matrix, \mathbf{M} via 238 $\mathbf{M} = \mathbf{I}_{t' \times t'} \otimes \mathbf{L}$. By multiplying the nt' vector of genomic values (**u**) by the inverse of **M**, we are 239 provided with a vector of transformed genomic values $(\mathbf{u}^* = \mathbf{M}^{-1}\mathbf{u})$ that follow a distribution given by 240 $N(0, \Sigma_{g} \otimes I_{n \times n})$. Thus, the transformed genomic values are independent between accessions. 241

BN are a class of graphical models that represent the probabilistic dependencies between a set of random variables as a directed acyclic graph (\mathscr{G}) (Scutari and Denis, 2014). \mathscr{G} is composed of nodes (V) that represent random variables and edges (E) that depict probabilistic dependencies between nodes. BN follow the Markov property, which states that given its parents, a node is conditionally independent of all nodes that are non-descendants (Scutari and Denis, 2014). The joint probability distribution for krandom variables ($X_V = (X_1, ..., X_k)$) is given by

$$P(X_V) = P(X_1, ..., X_k) = \prod_{V=1}^k P(X_V | \Pi_{X_V})$$

where parent nodes to X_v is indicated by Π_{X_V} (Scutari and Denis, 2014).

The vector of transformed genomic values (\mathbf{u}^*) was used as input for BN learning using the **bnlearn** 243 package (Scutari, 2009). Structure learning was performed using four algorithms: hill-climbing (HC), 244 tabu-search, max-min hill-climbing (MMHC), and general 2-phase restricted maximization (RSmax2). 245 HC and tabu are score-based, greedy algorithms which seek to maximize the goodness-of-fit (i.e., network 246 score). These algorithms begin with an empty network structure and add, remove, or reverse edge each 247 edge until a maximum score is reached. The latter two algorithms, MMHC and RSmax2, are hybrid 248 learning algorithms, which essentially restrict the score-based approach described above on a subset of 249 nodes within the network (Tsamardinos et al., 2006). For each algorithm, we used a combination of 250 bootstrapping and model averaging to identity robust networks and quantify uncertainty in linkages and 251 the direction of each edge. Five hundred bootstrapping replicates were used and edges that were present 252 in less than 85% of the networks were removed, and the models were averaged. We compared networks 253 from each algorithm using the Bayesian information criteria (BIC) and selected the 'best' network 254 according to the network that produced the highest BIC since BNlearn rescales BIC values by -2. 255

Genomic structural equation model

Work by Gianola and Sorensen (2004) provided a basis to introduce SEM into classical quantitative genetics frameworks. SEM utilize a system of linear equations to model the interrelationships between multiple dependant variables. Once introduced into the quantitative genetics frameworks pioneered by Henderson (1984), these approaches provide a means to partition multiple phenotypes into direct and indirect genetic components according to a predefined network structure (Gianola and Sorensen, 2004; Valente et al., 2013; Bello et al., 2018). In matrix form, the structural equation model is given by

$$\mathbf{Y} = \mathbf{A}\mathbf{Y} + \mathbf{X}\mathbf{b} + \mathbf{Z}\mathbf{u} + \mathbf{e}$$

where all matrices are defined according to the MTM described above. However, note that the response ²⁵⁷ variable **Y** appears on both the right and left-hand side of the equation, meaning that some phenotypes ²⁵⁸ will serve as covariates for other phenotypes. The effect of an upstream phenotype on a downstream ²⁵⁹ phenotype is determined by the direction and magnitude of elements in the coefficient matrix (Λ). Λ is ²⁶⁰ typically a lower triangle matrix with zeros in the diagonal and upper triangle. We assume ²⁶¹ $\mathbf{u} \sim N(0, \Sigma_{u_0}) \otimes \mathbf{G})$ and $\mathbf{e} \sim N(0, \Sigma_{e_0} \otimes \mathbf{I}_{n \times n})$, where Σ_{u_0} and Σ_{e_0} represent the genomic and residual ²⁶² covariances for total effects. ²⁶³

Given a simple, hypothetical causal structure for three phenotypes $(y_1 \rightarrow y_2 \text{ and } y_1 \rightarrow y_3)$, we can decompose each phenotype into genetic and non-genetic components using the following system of equations 266 266 266 266 266

 $\begin{aligned} \mathbf{y_1} &= \mathbf{X}\mathbf{b} + \mathbf{Z}\mathbf{u_1} + \mathbf{e_1} \\ \mathbf{y_2} &= \lambda_{y_1 \to y_2}\mathbf{y_1} + \mathbf{X}\mathbf{b} + \mathbf{Z}\mathbf{u_2} + \mathbf{e_2} \\ \mathbf{y_3} &= \lambda_{y_1 \to y_3}\mathbf{y_1} + \mathbf{X}\mathbf{b} + \mathbf{Z}\mathbf{u_3} + \mathbf{e_3} \end{aligned}$

Since y_1 has no variables leading to it, the total genomic effects for y_1 are given by $\mathbf{u}_{\mathbf{1}_{total}} = \mathbf{u}_1$. For 267 y_2 we have an indirect effect coming from y_1 , therefore the total genomic value is given by 268 $\mathbf{u}_{2_{\text{total}}} = \lambda_{y_1 \to y_2} \mathbf{u}_1 + \mathbf{u}_2$. For y_3 , total genomic values are given by $\mathbf{u}_{3_{\text{total}}} = \lambda_{y_1 \to y_3} \mathbf{u}_1 + \mathbf{u}_3$. Solving the 269 mixed model equation provides solutions for direct genomic values and estimates the genetic and residual 270 (co)variances for direct effects among traits (Σ_{u_0} and Σ_{e_0} , respectively). Covariances for total genomic 271 and residual effects can be computed through a simple transformation on the appropriate covariances 272 matrix for direct effects. The total genomic covariance is given by $\Sigma_{g} = (\mathbf{I}_{t \times t} - \mathbf{\Lambda})^{-1} \Sigma_{u_0} (\mathbf{I}_{t \times t} - \mathbf{\Lambda})^{-1'}$. 273 We fit SEM using the ten latent environmental variables and the plasticity measures for three empirical 274 phenotypes according to the learned structure described above. The model was fit using the MTM package 275 with 10,000 MCMC samples with the first 2,000 samples discarded and every fifth sample retained 276 (de los Campos and Grüneberg, 2016). 277

Data availability

Local environmental variables were obtained from the Arabidopsis ClimTools repository	279
(https://github.com/CLIMtools) (Ferrero-Serrano and Assmann, 2019), and empirical phenotypes for	280
common garden locations were obtained from Exposito-Alonso et al. (2019). Scripts used for analyses of	281
these data are available Arabidopsis EFA repository	282
(https://github.com/malachycampbell/ArabidopsisEFA) and are documented to ensure	283
reproducibility. Supplemental figures and files are available at FigShare ().	284

Results

To examine the genomic relationship between local environments across the native range of Arabidopsis 286 thaliana we utilized a publicly available panel of 1,135 diverse Arabidopsis accessions. These materials 287 were collected from 829 non-redundant sites across Europe, Asia, Africa and N. America, and are 288 discussed in detail by Ferrero-Serrano and Assmann (2019). The collection site for each accession is 289 provided as Supplemental Figure S1. We utilized an existing dataset of 205 climatic, edaphic, and 290 remote sensing variables to characterize the local environmental conditions at each of the collection sites. 291 These variables describe precipitation, temperature, and vegetative productivity patterns, as well as soil 292 physical and chemical characteristics (Ferrero-Serrano and Assmann, 2019). 293

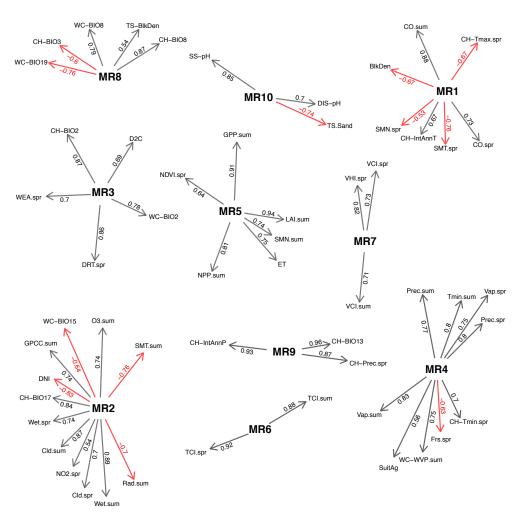


Figure 1. Factor loadings for manifest local environmental variables. Variables in bold type face are latent factors identified using factor analysis, while nodes emanating from these are manifest environmental variables. Edges colored in grey indicate the manifest variable has a positive loading on the latent factor, while those in red indicate negative loadings.

Factor analysis reveals the underlying structure of local environments

An initial inspection of the environmental variables showed a high degree of correlation between variables 295 (Supplemental Fig. S2). Given the size of the data set, as well as the high degree of correlation between 296 variables, we sought to reduce the 55 variables to a smaller set of factors that capture the underlying 297 theoretical structure of the environments. To this end, we performed EFA on the set of 55 variables to 298 explore the underlying structure of local environmental conditions and define a reduced set of variables 299 that capture unobserved processes (latent factors) that drive these relationships. Confirmatory factor 300 analysis was used to determine the contribution of each environmental variable to the latent factor and 301 quantify how each accession contributed to each latent factor. EFA revealed that the 55 variables could 302 be reduced to a set of 11 latent factors (Supplemental Fig. S3). Although 11 latent factors were defined, 303 variables loading onto factor 11 had stronger loading on other latent factors. Thus this latent factor was 304 omitted from downstream analysis. The loadings from EFA are provided as Supplemental File S1. 305

In theory, these latent factors should represent unobserved processes that give rise to the observed 306 variables, and in the context of the current study, may describe processes that shape local environments. 307 Factor loadings from CFA are shown in Figure 1. A complete listing of latent factors, the manifest 308 variables that load onto them, and the interpretation of latent factors is provided in Supplemental File 309 S2. Twelve environmental variables loaded onto the second latent factor (MR2). The manifest variables 310 describe the frequency of wet days, cloud coverage, solar radiation, precipitation seasonality and 311 precipitation of the driest quarter. Variables associated with precipitation and cloud cover largely 312 showed positive contributions to MR2, while those associated with solar radiation showed negative 313 contributions. Thus, MR2 is likely a description of how bright and dry an environment is. Three latent 314 factors were defined which captured the favorability of local environments to plant growth. For instance, 315 two metrics for vegetation condition index (VCI) which quantifies vegetation cover in a period of time to 316 relative extremes and vegetative health index (VHI) that represents the favorability of the environment 317 for vegetation activity showed positive loadings onto onto MR7. Moreover, the two manifest variables 318 that represent temperature condition index (TCI) which loaded positively onto MR6. While MR6 and 319 MR7 are largely associated with indices that describe the potential impact of environmental conditions 320 on plant health, MR5 captures the productively of the environment as manifest variables associated with 321 gross primary productivity, evapotranspiration, normalized difference vegetation index, and net primary 322 productivity were loaded onto this latent factor. Several other latent factors were identified that 323 captured precipitation patterns at each local environment. For instance, the ninth latent factor (MR9) 324 largely captures precipitation and precipitation variability between years. Environmental variables 325 representing the amount of precipitation in the wettest month, precipitation in the spring, and 326 interannual precipitation showed strong positive contributions to MR9. 327

Examining plasticity in fitness and phenology in contrasting environments

The ability of plants to exhibit plasticity in phenotypic traits is important strategy for adaptation to 329 environmental constraints. With this in mind, we sought to elucidate the genetic interrelationships 330 between plasticity in phenological traits and fitness, and local environmental characteristics. We utilized 331 an existing dataset consisting of phenological (time to germination and flowering) traits and fitness 332 recorded on 515 diverse Arabidopisis accessions grown in common garden experiments in Tuebingen and 333 Madrid (Exposito-Alonso et al., 2019). At each common garden location, accessions were grown under 334 simulated high and low rainfall conditions, with high rainfall conditions mimicking the natural 335 precipitation in Tuebingen and low rainfall conditions mimicking the precipitation at Madrid 336 (Exposito-Alonso et al., 2019). 337

The distribution of phenological and fitness traits at each precipitation-location combinations are 338 shown in Figure 2. Significant differences between precipitation-location combinations were observed for 339 fitness and flowering time (p < 0.0001). In general, accessions flowered later at Tuebingen compared to 340 Madrid, while low precipitation seemed to delay flowering in both locations indicating that temperature 341 and daylength differences between locations may be the largest driver of differences in flowering time 342 between locations. In general, the accessions exhibited higher fitness in the two high-rainfall treatments 343 compared to low rainfall treatments. Fitness was highest for the high rainfall treatment in Madrid, while 344 the low precipitation treatment at Madrid showed the lowest average fitness. The environment in the 345 high rainfall treatment at Madrid is characterized by simulated rainfall that is similar to the natural 346 precipitation at the common garden location in Tuebingen. Thus, the ample water availability (27.8% 347 SWC) combined with the warm temperatures (median temperature 8.5° C) in Madrid are highly 348 favorable for growth and reproduction in Arabidopsis. However, when warm temperatures are combined 349 with inadequate rainfall (16.1% SWC), the overall performance is reduced greatly, as observed for the 350 low average fitness observed in low precipitation in Madrid (M_1) . 351

To estimate environmental plasticity for fitness and phenological traits, we estimated reaction norms for each accession using the FW approach (Finlay and Wilkinson, 1963). Briefly, the FW approach expresses the plasticity for each individual grown across a range of environments as a function of the average population performance at each environment. For each individual, the slope of the linear model expresses the plasticity (or macroenvironmental sensitivity) with respect to average plasticity of the population. The plasticity for each accession with respect to mean performance at each environment is shown in Figure 2D-F.

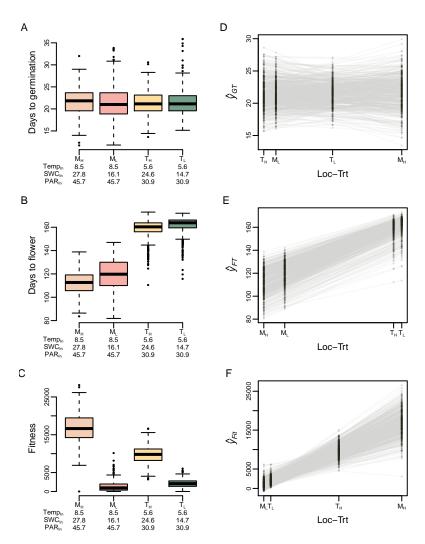


Figure 2. Distribution and plasticity of fitness and phenological traits across contrasting environments. (A-C) Distribution of adjusted means for fitness and phenological traits. Median values for environmental conditions within shelters are shown beneath each boxplot. Temp refers to median temperature in °C, SWC indicates soil water content, and PAR refers to photosythetically active radiation (mol m⁻² day⁻¹). The predicted phenotypic values (\hat{y}) of each accession in each location-treatment (Loc-Trt) combination is shown in panels D-F and were obtained using the FW approach. 'M' refers to common garden in Madrid and 'T' indicates common garden in Tuebingen, while the subscripts _L and _H refer to the low and high precipitation treatment, respectively.

Elucidating genetic dependencies between local environmental factors and fitness related traits

To elucidate the genetic interdependencies between local environmental conditions, and fitness and phenological plasticity, we inferred the potential causal genetic relationships between environmental

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factors and observed phenotypes using four BN structure learning algorithms. Structure learning was performed using the ten latent environmental factors described above and reaction norm slopes for phenological traits and fitness, and the "best" structure was selected based on BIC scores. Of the four algorithms evaluated, the "best" network was given by tabu algorithm (Table 1). Since the primary objective of this study is to elucidate the relationships between local environmental conditions and empirical phenotypes, we focused interpretations of the network on relationships within the Markov blanket for plasticity traits (Figure 3).

Table 1. Evaluation of four Bayesian structure learning algorithms. Bayesian network structures were learned using the ten latent environmental variables and plasticity for phenological traits (germination and flowering time) and fitness. The "best" network was selected based on the highest Bayesian information criteria (BIC) and Gaussian BIC values (gBIC). Algo.: algorithm; HC: hill-climbing; MMHC: min-max hill-climbing; RSmax2: general 2-phase restricted maximization

Algo.	gBIC	BIC
HC	-1963.02	-1963.02
tabu	-1962.58	-1962.58
MMHC	-2480.54	-2480.54
RSmax2	-2681.40	-2681.40

Although the learned structure is complex, several interesting features are apparent. First, of the 29 370 edges in the network, 41.4% (12 edges) describe relationships from environmental variables to empirical 371 phenotypes, while only 3.45% (1 edge) describe relationships from plastic responses to environmental 372 variables. These results suggest that genomic values for empirical phenotypes are highly dependent on 373 genetic factors associated with adaptation to local environmental conditions. In addition, 51.7% edges 374 (15 edges) were from environmental variables to other environmental variables, and only a single edge 375 was from plastic responses to other plastic responses. Thus, genetic relationships between environmental 376 variables or plastic responses are far more common than relationships from plastic responses to 377 environmental variables. 378

In addition to overall topological features of the BN, several nodes were identified that were heavily 379 influenced by other variables. For instance, plasticity in flowering time (FT) showed the largest number 380 of indirect effects, suggesting that plasticity in flowering time is highly dependent on genetic effects from 381 adaptation to local environments. A total of seven variables were leading to FT, while three were leading 382 to both plasticity in germination time (GT) and fitness (Fit). Several variables were identified that had 383 indirect effects on many variables. For instance, MR5 and MR9, which describe overall plant 384 productivity, and precipitation and interannual precipitation variability, respectively, each showed 385 indirect effects on four nodes. 386

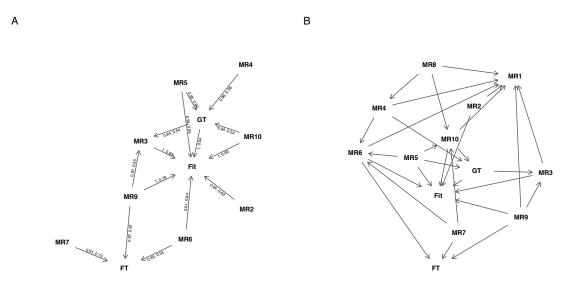


Figure 3. Visual depiction of probabilistic dependancies between environmental variables and empirical phenotypes. The network shown in panel A depicts the Markov blanket for empirical phenotypes and the full network is shown in panel B. A model averaging approach with 500 bootstrap samples was used to learn Bayesian network. The two numbers above each directed edge in panel A shows the proportion of bootstrap samples with the given edge and the proportion of samples with the given direction. The environmental variables are indicated with the "MR" prefix, while the empirical phenotypes are defined as follows: Fit: fitness plasticity; FT: flowering time plasticity; GT: germination time plasticity.

Structural equation modeling

The BN described above represents the probabilistic dependencies between plastic responses and local 388 environmental conditions (Scutari and Denis, 2014). While this approach may provide insights into how 389 variables act on one another, it does not tell how much of an effect one variable has on another. To 390 estimate the magnitude of direct (QTL acting directly on focal trait) and indirect (QTL effects 391 transmitted on focal trait by upstream trait) relationships among variables, we performed SEM using the 392 learned structure described above. We leveraged this approach to decompose total genomic values for 393 each environmental variable and empirical phenotype into direct and indirect effects, and examine the 394 covariance between total genomic values and direct genomic values. The matrix of structural equation 395 coefficients is shown in Table 2, and the genomic correlation matrix of direct and total effects is shown in 396 Figure 4. 397

The utilization of plastic responses for phenological traits was motivated by several studies that ³⁹⁸ suggest changes in an individual's life cycle may be an important mechanism for adaptation to specific ³⁹⁹

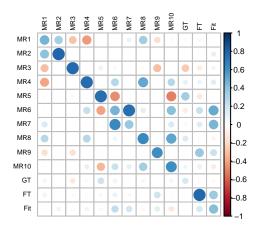


Figure 4. Genomic heritability and correlation for direct and indirect genetic effects The genomic heritability for total additive genetic effects (h^2) are shown in the diagonal. The upper triangle of the matrix shows the genomic correlation for total effects, while the lower triangle shows the genomic correlation for direct genetic values. Fit: fitness plasticity; FT: plasticity in flowering time; GT: plasticity in germination time

environmental constraints (Anderson et al., 2012; Vitasse et al., 2013; Augspurger, 2008; Chuine, 2010). 400 While total genomic covariances provide insight into the relationships between total genetic values for 401 two phenotypes, examination of the direct genomic covariances between traits may be more important in 402 the context of the current study, as the covariance of direct genomic effects is driven by QTL that have 403 an effect on both environmental adaptation and plasticity or QTL that affect each trait independently 404 but are in tight LD (Valente et al., 2013). For direct genomic effects, the strongest positive genomic 405 correlation between plastic responses and environmental variables was observed for Fit and MR6 406 $(r_{g_{direct}} = 0.24)$, which is a composite of temperature conditioning indices with lower values indicate a 407 potential for high temperature stress on vegetative biomass. Fit also showed positive direct genomic 408 correlation with MR7 ($r_{g_{direct}} = 0.18$), a variable composed of indices quantifying plant health, and MR9 409 $(r_{q_{direct}} = 0.13)$, which quantifies precipitation and interannual variability in precipitation. Collectively, 410 these results indicate that the accessions that harbor alleles for reduced sensitivity of fitness to 411 temperature gradients likely also harbor alleles associated with adaptation to warm, low rainfall 412 environments. 413

In addition to Fit, relatively strong positive direct genomic correlation was observed between FT and 414 MR9 ($r_{g_{direct}} = 0.20$), as well as GT and MR5 ($r_{g_{direct}} = 0.21$). However, the slope for FT largely 415 represents the sensitivity of flowering time to differences in photoperiod and/or temperature for an 416 accession, with lower values indicating more similar flowering times between common garden locations. 417

Table 2. Structural coefficients estimated using structural equation modeling. Path coefficients for network structure pictured in Figure 3 was estimated using a structural equation modeling approach. The columns indicate upstream nodes, while the rows indicate downstream nodes. Elements with '-' indicate pairs of nodes that are not linked by an edge. Coefficient matrices for structures learned using a Bayesian network approach are typically have zero elements in the diagonal and upper triangle, however the coefficient matrix below has been reordered so that environmental variables are grouped and ordered by name. Fit: fitness plasticity; FT: plasticity in flowering time; GT: plasticity in germination time. Variables with the 'MR' prefix indicate latent environmental variables.

	MR1	MR2	MR3	MR4	MR5	MR6	MR7	MR8	MR9	MR10	GT	\mathbf{FT}	Fit
MR1	-	0.35	-0.31	-0.47	-	0.13	-	0.6	-0.23	-0.18	-	-	-
MR2	-	-	-	-	-	-	-	-	-	-	-	-	-
MR3	-	-	-	-	-	-	-	-	-0.17	-	-0.2	-	-
MR4	-	-	-	-	-	-	-	0.38	-	-	-	-	-
MR5	-	-	-	-	-	-	-	-	-	-	-	-	-
MR6	-	-	-	0.23	-0.43	-	0.81	-	-	-	-	-	-
MR7	-	-	-	-	-	-	-	-	-	-	-	-	-
MR8	-	-	-	-	-	-	-	-	-	-	-	-	-
MR9	-	-	-	-	-	-	-	-	-	-	-	-	-
MR10	-	-	-	-	-0.33	-	0.12	0.41	-	-	-	-	-
GT	-	-	-	0.01	0.18	-	-	-	-	0.1	-	-	-
FT	-	-	-	-	-	0.13	-0.06	-	0.31	-	-	-	-
Fit	-	0.1	-0.01	-	0.13	0.34	-	-	0.13	-0.19	-	0.11	-

Therefore, it is unclear whether the non-zero direct genomic covariance between these variables indicates 418 a common mechanism, or potential confounding of photoperiod insensitive accessions originating from 419 more southern locations. 420

Discussion

Environment association analyses have become popular approaches to elucidate the genetic basis of local 422 adaptation in the absence of fitness measurements in multilocation common garden trials (Fournier-Level 423 et al., 2011; Yoder et al., 2014; Lasky et al., 2015). The aim of EAA is to identify genes or loci that may 424 impact traits that confer fitness along an environmental gradient. However, when fitness is measured in 425 multiple common garden locations along an environmental gradient, the change in fitness as a function of 426 mean population performance provides a single metric that describes the impact of the environment on 427 fitness. Moreover, when this metric is introduced as the response variable in genome-wide association 428 studies, strong associations indicate the presence of gene(s) that may influence fitness along the 429 environmental gradient. 430

In the current study, we seek to integrate both data types in the SEM framework to examine the 431 genetic interdependencies and covariances between changes in fitness and phenology in multiple 432 environments and local environmental conditions. However, whereas most EAA estimate the effects of 433 individual loci, we predict the total genetic values (i.e. the summation of QTL effects for a given 434 genotype) for each variable. Thus, in cases where collection sites and common garden locations follow the 435 same gradients, we expect covariance in genetic signals that impact both variables directly. Consistent 436 with this expectation, we observed non-zero genetic covariance between local environmental conditions 437 and changes in fitness between common garden locations. For instance, Fit showed positive correlation of 438 direct genetic effects for MR6, as well as MR7. The latent variables MR6 and MR7, capture the 439 favorably of the local environment for plant growth. Thus, higher values indicate environments that have 440 favorable conditions for plant growth and, on a whole, are highly productive. Moreover, Fit describes the 441 changes in fitness driven largely by water availability, with higher values indicating greater fitness in 442 high-rainfall treatment in Madrid and low values indicating low fitness in low-rainfall treatment in 443 Madrid (Figure 2). Thus, the positive genomic correlation of direct effects indicates that accessions 444 harboring alleles for high fitness in simulated, high-productivity environments will also tend to harbor 445 alleles associated with adaptation to highly productive local environments. Although weaker than the 446 direct genomic correlation for MR6 and MR7, Fit also showed positive genomic correlation with a latent 447 environmental variable that largely captured precipitation and precipitation variability of the local 448 environment, with higher values indicating higher precipitation (MR9; $r_{q_{direct}} = 0.13$). Collectively, these 449 results indicate that fitness in response to some local environmental conditions may be regulated common 450 genetic mechanisms that affect fitness in simulated environments. However in either case (e.g., local 451 environment associations or common garden fitness), the traits that impact fitness are largely unknown. 452

Phenotypic plasticity is an important process that allow plants to quickly modify physiology, morphology, or phenology in response to changes in the environment (Bradshaw, 1965). Individuals that exhibit greater plasticity may be better positioned to respond to new environmental constraints, as novel 455

phenotypes bought on by environmental change may provide persistence in the short-term 456 (West-Eberhard, 2005; Matesanz et al., 2010; Nicotra et al., 2010; Valladares et al., 2014). However, 457 phenotypic plasticity is not always advantageous (DeWitt et al., 1998; Ghalambor et al., 2007). For 458 instance, Scheepens and Stöcklin (2013) showed that increased temperature leads to early flowering, but 459 reduced seed set in *Campanula thyrsoides*. Thus, it is important to couple observations of plasticity 460 across an environmental gradient with measurements of fitness in the same environments to determine 461 whether phenotypic plasticity can be a mechanism underlying fitness. Here, we utilized measures of 462 fitness and empirical phenotypes in four environments. Correlations for reaction norms for fitness and 463 phenological traits showed a significant, albeit weak, correlations between Fit and GT (r = -0.09, p =464 (0.417) and Fit and FT (r = 0.18, p < 0.0001), indicating that these changes in fitness are associated 465 with changes in phenology. In the case of FT, the positive correlation indicates that accessions that show 466 greater plasticity in flowering time (positive slope for FT meaning delayed flowering in Germany relative 467 to Madrid) tend to exhibit greater fitness in high-precipitation regimes relative to low-precipitation 468 regimes (i.e., positive slope for Fit). Correlation provides a simple means to measure the relationships 469 between two traits within a population. However, a non-zero correlation does not necessarily indicate 470 that the outcome/expression for one characteristic is dependent on another. BN approaches on the other 471 hand, have been developed to elucidate probabilistic dependencies among a group of interrelated 472 variables (Pearl, 2014; Scutari and Denis, 2014). The BN shown in Figure 3 shows an directed edge from 473 GT to Fit, indicating that changes in fitness across the common garden environments is dependent on 474 changes in germination time. However, no edges were found between FT and Fit, indicating that 475 although these two characteristics covary, changes in Fit may not be dependent on changes in FT. 476

Although it is seemingly a natural tendency to view these dependencies as causal relationships, it is 477 important not to over interpret results from BN. While BN are a powerful approach to assess the 478 interdependencies between variables, structure learning with BN imposes several constraints that may 479 limit its applications in biology. One major limitation is that BN do not allow feedback loops or cyclical 480 relationships in the structure, which are pervasive throughout biology especially at a molecular level 481 (Scutari and Denis, 2014). Thus, if the underlying causal relationships between traits involves feedback 482 loops, the structure learned with BN will likely be inaccurate (Valente et al., 2013). Thus, the network 483 might reflect highly probable relationships between variables, but may not represent the true causal 484 relationships that give rise to the data. Secondly, in the current study, BN were constructed using a 485 mixture of observational and experimental data. In the absence of randomization, dependencies observed 486 in Bayesian networks constructed using observational data may be driven by unobserved confounders, 487 thereby making causal claims based on the data problematic (Bello et al., 2018, see for review). 488 Nevertheless, causal relationships can be learned from the data and should be used to generate 489 hypothesis for further studies. In our study, BN revealed dependencies between plasticity in fitness and 490

several environmental variables. Fitness in a given environment is largely the consequence of a trait or 491 traits that confer adaptation to a set of environmental conditions. In other words, fitness is not a 492 mechanism for local adaptation, but rather is a measure of adaptation. Thus, we expect that fitness in a 493 given location/precipitation regime should be highly dependent on mechanisms that were selected by 494 environmental pressures in the accessions' local environments, and this expectation is largely confirmed 495 by the network learned from the data (Figure 3). However, covariance in direct effects for other variables, 496 such as between FT and MR9, may not be so easy to explain. The latent environmental variable MR9 497 largely captures precipitation and precipitation variability, as the manifest variables spring precipitation, 498 precipitation of the wettest month, and interannual precipitation variability load onto MR9. The positive 499 direct covariance between MR9 and FT suggest that accessions that harbor alleles associated with 500 adaptation to environments with high precipitation will also tend to harbor alleles associated with higher 501 plasticity in flowering time. However, plasticity in flowering time is largely driven by differences in day 502 length and temperature between common garden locations rather than by precipitation regimes (Figure 503 2). Thus, it is questionable whether the direct genomic covariance is due to QTL that affect adaptation 504 to precipitation gradients and the sensitivity of flowering time to photoperiod and/or temperature, or if 505 this is driven by unaccounted, confounding effects within the data. Projection of phenotypic values for 506 FT on collection sites show clusters of accessions originating from the Northern Iberian peninsula and 507 Southern Sweden with low plasticity for flowering time (Supplemental Figure S4). Moreover, these 508 regions also exhibit low values for MR9. Further studies or alternative experimental designs are necessary 509 to determine whether this covariance is due to common effects on adaptation to precipitation gradients 510 and plasticity in FT, or are due to sampling bias. Thus, while BN can provide important insight into the 511 interrelationships between traits, when these networks are constructed using observational data we 512 should view these results with caution rather than to discount inferred relationships as spurious. 513

While BN describe the probabilistic dependencies among variables, they only provide insight into the 514 structure of relationships in the data. In many cases, we are interested in understanding how genetic 515 effects for an upstream trait affect the outcome of a downstream trait. SEM provides a means to 516 estimate path coefficients according to a predefined network structure, as well as partition phenotypic 517 values into genetic values that affect a trait directly (i.e., direct genetic values) and genetic values that 518 are due to genetic effects acting directly on upstream variables (Gianola and Sorensen, 2004; Valente 519 et al., 2013). In some sense, estimates of the structural coefficients may seem like the most attractive 520 component of SEM, as these describe how intervention on an upstream variable (e.g., a latent 521 environmental variable) will impact the outcome of the downstream variable (e.g., empirical phenotype) 522 given the direct effects for the downstream variable remain unchanged (Gianola and Sorensen, 2004). 523 However in the current study, we have data that is a combination of latent environmental variables and 524 empirical phenotypes. Thus, a more biologically meaningful question is whether QTL that have a direct 525

effect on adaptation to an environmental gradient also have a direct impact on some observable	526
phenotype. Non-zero covariance in direct effects between local environmental conditions indicates the	527
presence of common QTL, or independent QTL that are tightly linked (Valente et al., 2013). Thus,	528
identification of such QTL can provide important insights into the common mechanisms that impact	529
adaptation to local environments and plasticity.	530

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Supplemental Materials	534
• Supplemental Figure S1. Geographic locations for all 1,035 Arabidopsis accessions.	535
• Supplemental Figure S2. Heatmap for 55 manifest environmental variables.	536
• Supplemental Figure S3. Projection of phenotypic values for flowering time plasticity on collection sites for 515 accessions.	537 538
• Supplemental File S1. Factor loading from exploratory factor analysis.	539
• Supplemental File S2. Description of latent and manifest variables, and their loadings from confirmatory factor analysis.	540 541

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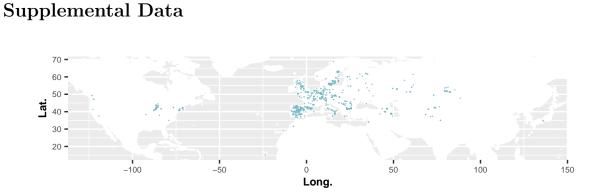


Figure S1. Geographic locations for all 1,035 Arabidopsis accessions. The locations for 1,035 accessions used to define latent environmental variables.

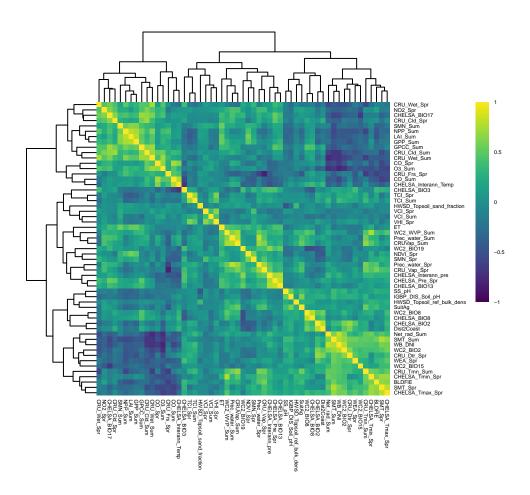
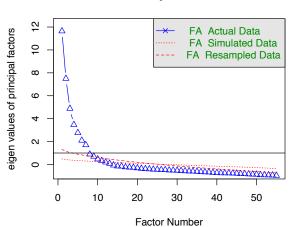


Figure S2. Heatmap for 55 manifest environmental variables. Spearman's method was used to generate the correlation matrix.



Parallel Analysis Scree Plots

Figure S3. Scree plot indicting the optimal number of latent factors for 55 environmental variables. Parallel factor analysis was performed using the psych package in R. This approach generates scree plots for the observed data and compares the results with scree plots generated from a random data matrix of the same size as the observed data set.

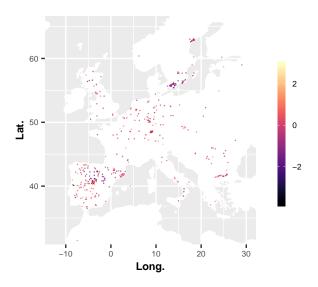


Figure S4. Projection of phenotypic values for flowering time plasticity on collection sites for 515 accessions. Higher plasticity values indicate a greater delay in flowering time Tuebingen relative to Madrid, and is indicated by the continuous color scale on the right. The red 'X' indicates the two common garden locations.